



Use of One-factor Design of Experiments (DOE) for Regression Modeling: A Robust Methodology

Soban Qadir Khan ^{a,b*} and Wan Muhamad Amir W. Ahmad ^a

^a *Unit of Biostatistics, School of Dental Sciences, Universiti Sains Malaysia (USM), Health Campus, 16150 Kubang Kerian, Kota Bharu, Kelantan, Malaysia.*

^b *Lecturer of Biostatistics, Department of Dental Education, College of Dentistry, Imam Abdulrahman Bin Faisal University, Kingdom of Saudi Arabia.*

Authors' contributions

This work was carried out in collaboration between both authors. Both authors read and approved the final manuscript.

Article Information

DOI: 10.9734/JPRI/2022/v34i25A35948

Open Peer Review History:

This journal follows the Advanced Open Peer Review policy. Identity of the Reviewers, Editor(s) and additional Reviewers, peer review comments, different versions of the manuscript, comments of the editors, etc are available here: <https://www.sdiarticle5.com/review-history/82304>

Original Research Article

Received 06 January 2022
Accepted 10 March 2022
Published 17 March 2022

ABSTRACT

In the present research era, high accuracy methods as a statistical analysis tool are increasing. Therefore, researchers are more focused to produce reliable and accurate results. Hence, the use of data modeling techniques is more focused to meet the needs of the current research trend. On the other hand, Design of Experiment (DOE) is extensively used among various scientific fields; however, its limitations do not allow these study designs for modeling purposes. Therefore, this study was designed to develop a methodology combining statistical methods that can provide to use one-factor DOE study designs for modeling and predictions. The addition of Fuzzy regression and multilayer feedforward (MLFF) neural network along with multiple linear regression would provide more accurate results with high accuracy. Furthermore, the developed methodology was tested on a dataset to test the methodology's performance and results provided that methodology provided regression models through MLR and fuzzy with high accuracy with the testing of the model's predictability through MLFF.

Keywords: *Design of experiment; Regression; Methodology; Robust; MLFF.*

*Corresponding author: E-mail: soban.qadir@student.usm.my;

1. INTRODUCTION

Design of experiment (DOE) study designs are widely used among various scientific and non-scientific experiments and can be used to explore or study the relationship or association among the variables [1-3]. However, the DOE study designs are made up of factors, and each factor is based on different categories [4]. Hence, due to the nature of the variables in DOE study designs, the data cannot be used directly for prediction purposes and some prior work is needed to be done before using the DOE study designs for regression modeling [5,6]. On the other hand, forecasting is becoming popular in the studies as it helps to improve the significance of the study findings and impact of the research; hence the use of regression modeling has become increasing among the scientific community.

Due to the nature of the variables in the DOE study designs, these study designs cannot be used directly for regression modeling. Hence, some prior work, which is called data transformation, is required to use DOE study designs for regression modeling [6]. Furthermore, due to the nature of the independent variables in the DOE study designs, called factors, it is likely to have fuzziness in the transformed data. On the other hand, linear regression models are designed to model crisp datasets, and their aptness becomes poor in

case of vague data [7]. Therefore, to address the issue of data fuzziness and incorporate fuzzy data into the regression model, a new approach in regression modeling was introduced, which is called Fuzzy linear regression modeling [8]. Like linear regression, which is based on probability theory, fuzzy regression is based on the theory of possibility [9,10]. L.A. Zadeh did the initial work on fuzzy regression, which later proceeded by Tanaka, Diamond, Ishibuchi and others [9,11,12].

Therefore, this study was designed to provide a methodology that can enable researchers to use their DOE study designs for prediction purposes. The study aim was to provide a comprehensive and robust methodology that included the transformation of one-factor DOE study design to linear form, use of bootstrapping to enhance the accuracy of estimated regression parameters, use of linear and fuzzy regression models and utilization of multilayer feedforwarding (MLFF) neural networking for model validation. In addition, demonstration of the methodology provided by fitting it on a secondary dataset.

2. METHODOLOGY

One factor DOE study design was used for transformation into linear form, followed by regression modeling and validation. Figure 1 illustrated the entire process involved in the methodology from the data transformation till the validation of the derived regression model.

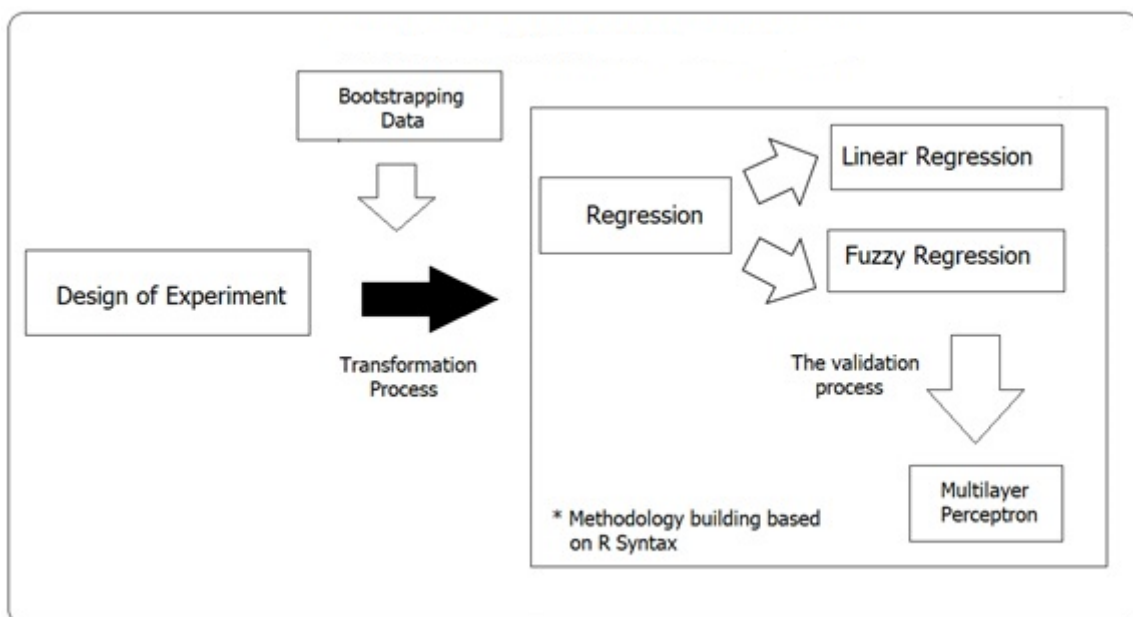


Fig. 1. Conceptual framework of methodology building

Therefore, the data transformation process on generalized one-factor DOE study design was initially elaborated. Hence, Table 1 introduced the distribution of one-factor DOE with i treatments and j observations within each treatment.

Data presented in table 1 has one dependent variable (y) and " i " treatments (factors). However, to transform the data into the linear form, " j "th treatment or factor was not required, as expressed in terms of $i-1$ treatments or factors

[13]. Therefore, a generalized matrix for the transformed dataset contained $r=i-1$ and $n=j$. Now the utmost part of the transformation process was to code the factor. The variables generated after the coding are called indicator variables that take on values 0, 1 or -1 [6]. This coding process must be done carefully because it led to the regression coefficients in the β vector. Hence, the matrix obtained after the transformation of the dataset had dependent and independent variables matrix, matrix for slopes and matrix for random error.

Table 1. General data distribution for one-factor study design

Treatment				
1	2	...		i
y_{11}	y_{21}	...		y_{i1}
y_{12}	y_{22}	...		y_{i2}
y_{13}	y_{23}	...		y_{i3}
.
.
.
y_{1i}	y_{2i}	...		y_{ii}

$$Y = \begin{bmatrix} Y_{11} \\ Y_{12} \\ \vdots \\ Y_{1n} \\ Y_{21} \\ Y_{22} \\ \vdots \\ Y_{in} \end{bmatrix}; X = \begin{bmatrix} 1 & 1 & 0 & \dots & 0 \\ 1 & 1 & 0 & \dots & 0 \\ 1 & 1 & 0 & \dots & 0 \\ 1 & 1 & 0 & \dots & 0 \\ 1 & 1 & 0 & \dots & 0 \\ 1 & 0 & 1 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 1 & -1 & -1 & \dots & -1 \end{bmatrix}; \beta = \begin{bmatrix} \mu. \equiv \beta_0 \\ \tau_1 = \beta_1 \\ \tau_2 = \beta_2 \\ \tau_3 = \beta_3 \\ \vdots \\ \tau_{i-1} = \beta_{i-1} \end{bmatrix}; \begin{bmatrix} \varepsilon_{11} \\ \varepsilon_{12} \\ \vdots \\ \varepsilon_{1n} \\ \varepsilon_{21} \\ \varepsilon_{22} \\ \vdots \\ \varepsilon_{in} \end{bmatrix}$$

Let x_{ij1} denoted the value of indicator variable x_1 , x_{ij2} indicated the value of indicator variable x_2 , and so on. Using $i-1$ indicators in the model and multiple linear regression (MLR) model could be stated as

$$Y_{ij} = \mu. + \tau_1 x_{ij1} + \tau_2 x_{ij2} + \dots + \tau_{i-1} x_{ij(i-1)} + \varepsilon_{ij} \text{ ----- (1)}$$

where,

$$x_{ij1} = \begin{cases} 1 & \text{if the case from the factor level 1} \\ -1 & \text{if the case from the factor level (i)} \\ 0 & \text{Otherwise} \end{cases}$$

$$x_{ij2} = \begin{cases} 1 & \text{if the case from the factor level 2} \\ -1 & \text{if the case from the factor level (i)} \\ 0 & \text{Otherwise} \end{cases}$$

$$x_{ij(i-1)} = \begin{cases} 1 & \text{if the case from the factor level (i - 1)} \\ -1 & \text{if the case from the factor level (i)} \\ 0 & \text{Otherwise} \end{cases}$$

1.1 A Case Study from Health Sciences

To apply the above process of data transformation to get the linear form, a one-factor DOE data was extracted from a book "Probability & Statistics for Engineers & Scientists" by Walpole R.E et al [14]. The dataset belonged to the pharmacological study in which different drugs were tested. The dataset

consisted of 25 patients with a fever of 38 degrees Celsius or higher and used five different brands of headache relief medications. The number of hours of headache relief was recorded in table 2.

Table 2. Hours of relief from five different brands of headache tablets

Drug 1	Drug 2	Drug 3	Drug 4	Drug 5
5.2	9.1	3.2	2.4	7.1
4.7	7.1	5.8	3.4	6.6
8.1	8.2	2.2	4.1	9.3
6.2	6.0	3.1	1.0	4.2
3.0	9.1	7.2	4.0	7.6

After that, the transformation process was initiated; data in table 2 had five groups ($r = 5$) and five observations in each group ($n = 5$). Hence, each column of the transformed matrix had 25 observations ($r \times n$). The independent variables' matrix required indicator variables with values 0, 1 and -1. Therefore, the matrix after transformation looked like this:

$$Y = \begin{bmatrix} Y_{11} \\ Y_{12} \\ Y_{13} \\ Y_{14} \\ Y_{15} \\ Y_{21} \\ \vdots \\ Y_{55} \end{bmatrix}; X = \begin{bmatrix} 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots \\ 1 & -1 & -1 & -1 & -1 \end{bmatrix}; \beta = \begin{bmatrix} \mu. \equiv \beta_0 \\ \tau_1 = \beta_1 \\ \tau_2 = \beta_2 \\ \tau_3 = \beta_3 \\ \tau_4 = \beta_4 \end{bmatrix}; \begin{bmatrix} \varepsilon_{11} \\ \varepsilon_{12} \\ \varepsilon_{13} \\ \varepsilon_{14} \\ \varepsilon_{15} \\ \varepsilon_{21} \\ \vdots \\ \varepsilon_{55} \end{bmatrix}$$

Let x_{i1} denoted the value of indicator variable x_1 , x_{i2} indicated the value of indicator variable x_2 , etc. Using $t-1$ indicators in the model and multiple linear regression model for the study would be stated as

$$Y_i = \mu. + \tau_1 x_{i1} + \tau_2 x_{i2} + \tau_3 x_{i3} + \tau_4 x_{i4} + \varepsilon_i \text{ ----- (2)}$$

Where

$$x_{i1} = \begin{cases} 1 & \text{if the case from the factor level 1} \\ -1 & \text{if the case from the factor level 5} \\ 0 & \text{Otherwise} \end{cases} \quad x_{i2} = \begin{cases} 1 & \text{if the case from the factor level 2} \\ -1 & \text{if the case from the factor level 5} \\ 0 & \text{Otherwise} \end{cases}$$

$$x_{i3} = \begin{cases} 1 & \text{if the case from the factor level 3} \\ -1 & \text{if the case from the factor level 5} \\ 0 & \text{Otherwise} \end{cases} \quad x_{i4} = \begin{cases} 1 & \text{if the case from the factor level 4} \\ -1 & \text{if the case from the factor level 5} \\ 0 & \text{Otherwise} \end{cases}$$

Table 3 represented the data after transformation. The data had one dependent variable y_{ij} , and four x_{i1} , x_{i2} , x_{i3} , and x_{i4} . Data now transformed to linear form and could be used for regression modeling.

Table 3. Regression approach to one-factor DOE

y_{ij}	x_{i1}	x_{i2}	x_{i3}	x_{i4}
5.2	1	0	0	0
4.7	1	0	0	0
8.1	1	0	0	0
6.2	1	0	0	0
3.0	1	0	0	0
\vdots	\vdots	\vdots	\vdots	\vdots
4.2	-1	-1	-1	-1
7.6	-1	-1	-1	-1

Hence, data tabulated in table 3 showed a transformed form of one-factor DOE into linear. Therefore, this can be used for regression modeling. Thus, the R-software was used for writing syntax for regression modeling. In this developed methodology, to enhance the accuracy of estimated regression parameters, the syntax for bootstrapping was utilized first after the data entry into the R. The reason of using bootstrapping in the syntax was this technique was developed to increase the size of the sampled data by random replication process. Therefore, this technique could help to improve the accuracy of the outcome obtained from the methodology. The syntax for data splitting was followed by bootstrapping, which provided an opportunity to have another (independent) dataset that could be used to test the developed regression model. Hence, the syntax for data splitting was used to get "train" and "test"

datasets in 70:30 ratio. After that, the syntax for multiple linear regression and fuzzy regression was used by using "train" data, and the mean square error (MSE) for the model was calculated by using "test" data. To further validate the model and to check how far the model's prediction was from reality, the syntax for multilayer feedforward neural network (MLFF) was used. Since normalization was necessary before performing neural networks, the syntax for data normalization utilized prior neural networks [15]. Furthermore, normalized data were split into "train" and "test", in which "train" data was used for building the architecture of the neural network and "test" data used to test the predictability of the developed network. Therefore, comprehensive, combined and robust methodology with R-syntax by using the data in table 3 was as follows:

1.2 R Syntax for Modeling DOE Study Designs

```
y = c(5.2, 4.7, 8.1, 6.2, 3.0, 9.1, 7.1, 8.2, 6.0, 9.1, 3.2, 5.8, 2.2, 3.1,
      7.2, 2.4, 3.4, 4.1, 1.0, 4.0, 7.1, 6.6, 9.3, 4.2, 7.6)
x1 = c(1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1,
      -1, -1, -1)
x2 = c(0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, -1,
      -1, -1, -1)
x3 = c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, 0, 0, 0, 0, 0, -1,
      -1, -1, -1)
x4 = c(0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 1, 1, 1, 1, 1, -1,
      -1, -1, -1)
```

```
X = cbind(x1,x2,x3,x4)
data = data.frame(y,x1,x2,x3,x4)
```

R Syntax for data entry and Bootstrapping

#!/Performing Bootstrap for 1000

```
mydata <- rbind.data.frame(data, stringsAsFactors = FALSE)
iboot <- sample(1:nrow(mydata),size=1000, replace = TRUE)
bootdata <- mydata[iboot,]
```

R Syntax for splitting booted data into test and train data

```
#!/Randomly split the data into 70:30
#70 percent of the data at our disposal to train the network
#30 percent to test the network/
```

```
smp_size <- floor(0.70*nrow(bootdata))
set.seed(123)
train_ind<- sample(seq_len(nrow(bootdata)), size=smp_size)

train <- data.frame(bootdata[train_ind,])
test <- data.frame(bootdata[-train_ind,])
```

Print Data

```
print(train)
print(test)
```

R Syntax for MLR Regression Modeling

/Fit a Linear Regression Model

Use Mean Squared Error (MSE) as a Measure of Prediction Performance/

##Predict the Values for the Test Set and Calculate the MSE/

```
Model <- lm(y~x1+x2+x3+x4, data=train)
summary(Model)
predict_lm <- predict(Model,test)
MSE_lm <- sum((predict_lm - test$y)^2)/nrow(test)
MSE_lm
```

Syntax for Fuzzy regression Modeling

```
if(!require(fuzzyreg)) install.packages("fuzzyreg", dependencies = TRUE)
library(fuzzyreg)
```

##Fuzzy linear model using the PLRLS method##

```
f <-fuzzylm(y ~ x1+x2+x3+x4, data=train$lee, method = "plrIs", fuzzy.left.x = NULL, fuzzy.right.x =
NULL, fuzzy.left.y = NULL, fuzzy.right.y = NULL)
coef(f)
```

R Syntax for data normalization and Multilayer Feedforward Neural Network

##Performing neural network

##install the neuralnet package/

```
if(!require(neuralnet)){install.packages("neuralnet")}
library("neuralnet")
```

##Scaling the data for normalization

Method (usually called feature scaling) to get all the scaled data

in the range [0,1]/

```
max_data <- apply(bootdata, 2, max)
min_data <- apply(bootdata, 2, min)
data_scaled <- scale(bootdata,center = min_data, scale = max_data - min_data)
```

##Randomly split the data into 70:30

##70 percent of the data at our disposal to train the network

##30 percent to test the network/

```
index = sample(1:nrow(bootdata),round(0.70*nrow(bootdata)))
train_data <- as.data.frame(data_scaled[-index,])
test_data <- as.data.frame(data_scaled[-index,])
```

##Build the network

##Create 2 hidden layers have 3 and 2 neurons respectfully

##Input layer = 4

##Output layer = 1/

```
n = names(bootdata)
f = as.formula(paste("y ~", paste(n[!n %in% "y"], collapse = " + ")))
nn = neuralnet(f,data=train_data,hidden=c(3,2),linear.output=T)
plot(nn)
```

```
options(warn=-1)
```

```
#/30 percent of the available data to do this:  
#using first 4 columns representing the input variables  
#of the network and 1 is the output for NN/  
predicted <- compute(nn,test_data[,1:4])
```

```
#/Use the Mean Squared Error NN (MSE-forecasts the network) as a measure of how far away  
our predictions are from the real data/
```

```
MSE.net <- sum((test_data$y - predicted$net.result)^2)/nrow(test_data)  
MSE.net
```

```
#/Printing the Value of MSE for Linear Model and Neural Network/  
print(paste(MSE.lm,MSE.net))
```

3. RESULTS

The outcome generated from data after running the R syntax was summarized in this section. Parameters for multiple linear regression were calculated first with the summary of the model. Table 4 summarizes the output for the MLR estimated parameters. Slopes for the parameters x_2 , x_3 and x_4 were statistically significant ($p < 0.001$). However, because the data belonged to DOE study design hence all indicator variables must be included in the regression modeling to accurately reflect the data. Therefore, all indicator variables were included to model the data (Equation 3). Hence, a multiple linear

regression model with estimated parameters could be written as

$$\text{Hours of relief} = 5.56 - 0.104 x_1 + 2.55 x_2 - 2.43 x_3 - 2.03 x_4 \text{ ---- (3)}$$

The model was statistically significant ($p < 0.0001$), and the adjusted R-square was 0.71 (Table 5). To determine the predictability of the MLR model, the MSE (mean square error) of the model was computed, and it was found to be 1.05 (Table 5). Similarly, table 6 tabulated the parameters obtained for fuzzy regression, containing Central, lower and upper boundary values for intercept and variable.

Table 4. Parameter Estimates of Regression Modeling

Parameter Estimates				
Variable	Parameter Estimate	Standard Error	t-value	P-value
Intercept	5.56	0.15	35.87	<0.0001
x_1	-0.104	0.315	-0.329	0.235
x_2	2.55	0.306	8.304	<0.0001
x_3	-2.43	0.325	-7.473	<0.0001
x_4	-2.03	0.325	-6.244	<0.0001

Table 5. MLR Model Summary

Residual SE	1.279	R-Square	0.727
MSE	1.05	Adj R-Sq	0.71
F-statistic	43.36	P-value	<0.0001

Table 6. Parameter Estimates of Fuzzy Modeling

Parameter Estimates			
Variable	Central Tendency	Lower Boundary	Upper Boundary
Intercept	5.51	3.68	6.78
x_1	-0.007	-0.68	1.32
x_2	2.32	2.32	2.32
x_3	-1.15	-1.48	0.42
x_4	-2.68	-2.68	-2.68

To draw the fuzzy regression equation, a central tendency column was used. However, lower and upper boundary columns were used from table 6 to construct the equation for lower and upper boundaries for boundaries of fuzzy regression. Therefore, the fuzzy regression equations were as follow :

Central tendency of the fuzzy regression model:
 Hours of relief = $5.51 - 0.007 x_1 + 2.32 x_2 - 1.15 x_3 - 2.68 x_4$ ----- (4)

Lower boundary of the model support interval:
 Hours of relief = $3.68 - 0.6845 x_1 + 2.32 x_2 - 1.48 x_3 - 2.68 x_4$ ----- (5)

Upper boundary of the model support interval:
 Hours of relief = $6.78 + 1.32 x_1 + 2.32 x_2 + 0.42 x_3 - 2.68 x_4$ ----- (6)

To quantify how close the predicted values of the dependent variable (y) through each model (MLR and Fuzzy), the equations derived above, from MLR (Equation 3) and fuzzy (Equation 4), were

used on test data to calculate values for predicted y (Table 7). Furthermore, the absolute difference between original and predicted y from each model was computed to calculate the numeric difference between original and predicted values of the dependent variable through each model.

MLFF neural network was embedded in the syntax to test the strength of the parameters used in the regression model; therefore, it helped to determine how good the forecasting was through the derived regression model. Figure 2 presented the architecture of the neural network obtained from the data. The figure had hidden layers with 3 and 2 neurons, respectively, and as the networking was Feedforward, the information was only carried in the forward direction (Fig. 2). Furthermore, the calculated MSE for the network was 0.09. As a result, all four independent variables were good predictors of hours of headache relief after taking medicine.

Table 7. Predicted values of Y form MLR and fuzzy models

y	Predicted y		Abs difference	
	MLR	Fuzzy	MLR	Fuzzy
9.1	7.5791	7.027	1.5209	2.073
4.2	3.128	4.36	1.072	0.16
6.6	3.528	2.83	3.072	3.77
7.1	7.5791	7.027	0.4791	0.073
6.6	3.528	2.83	3.072	3.77
.
.
5.8	8.1089	7.83	2.3089	2.03
9.1	8.1089	7.83	0.9911	1.27
8.1	7.5791	7.027	0.5209	1.073
Average			2.16	2.01

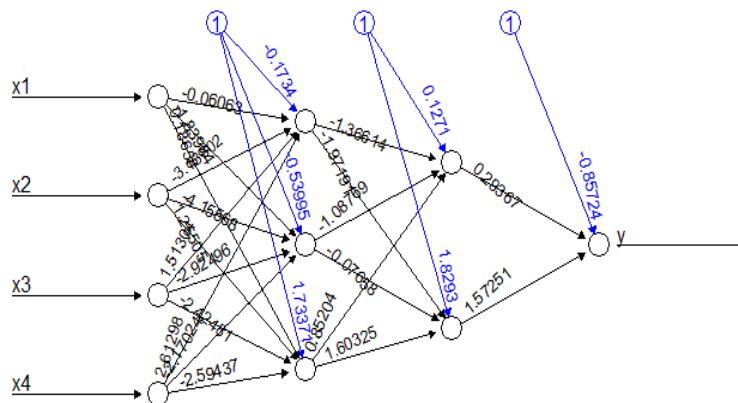


Fig. 2. The architecture of the MLFF neural network with four input variables, two hidden layers and one output node

4. DISCUSSION

In the present research era, research community is more intended to use data modeling techniques to improve the outcome of the research. Impact of the research could perhaps increase if study could predict future trends because it would increase the usability of the research work. However, due to the nature of some variables, they cannot be used for regression modeling unless transformed [6]. The independent variables in DOE study designs, which usually called factors, are collected in the form of categories [4]. Therefore, these study designs cannot be used for regression modeling without transformation. Hence, this study was aimed to develop a methodology (WAN-SOB's method) which could enable research community to use DOE study designs for regression modeling.

The key step towards the use of DOE study designs for regression modeling is the data transformation. Hence, the process of the transformation of one-factor DOE to linear form was provided in detail. This transformation process adopted from the previous study [13]. Therefore, linearity in the data generated as a result of data transformation.

Linear regression approach for data modeling is very common. However linear regression perhaps performed better with crisp datasets [16] if the underlying relationship were not a crisp function of a given form, the model's accuracy could be questioned [17]. Consequently, to counter the vagueness or fuzziness of the data in the regression modeling, fuzzy regression outperforms linear regression [18]. Therefore, fuzzy regression was used in the methodology along with linear regression and predicted values of dependent variable from each regression model (linear and fuzzy) was calculated. The difference between actual and predicted values from linear and fuzzy revealed that fuzzy regression provided that predictability of fuzzy regression was better than linear regression.

In addition, to further validate the derived regression model, MLFF neural network was used in the methodology. Studies had been used the neural network for validation of derived regression models and their predictability [19,20]. Ahmed et al. used neural networking for the validation of derived regression model and provided that small error from the neural network suggested the high accuracy and predictability of

the model [21]. In the present study, the calculated MSE from neural network was very small which suggested the high accuracy of the derived regression model.

5. CONCLUSION

This study provided a combined, comprehensive and robust methodology (Wan-SOB's Method) for using one-factor DOE for prediction purposes by transforming DOE into a linear form. Therefore, this methodology can allow the research community and academicians to use their DOE study designs for prediction purposes to meet the growing needs of research trends and help them get more improved outcomes from their research.

CONSENT

It is not applicable.

ETHICAL APPROVAL

It is not applicable.

COMPETING INTERESTS

Authors have declared that no competing interests exist.

REFERENCES

1. Gu S, Wang X, Shi L, Sun Q, Hu X, Gu Y, Sun X, Dong H. Health-related quality of life of type 2 diabetes patients hospitalized for a diabetes-related complication. *Quality of Life Research*, 2020;29(10): 2695-704.
2. Memon J, Holakouie-Naieni K, Majdzadeh R, Yekaninejad MS, Garmaroudi G, Raza O, Nematollahi S. Knowledge, attitude, and practice among mothers about newborn care in Sindh, Pakistan. *BMC Pregnancy and Childbirth*. 2019;19(1):1-9.
3. Hamid SK, Al-Dubayan AH, Al-Awami H, Khan SQ, Gad MM. In vitro assessment of the antifungal effects of neem powder added to polymethyl methacrylate denture base material. *Journal of Clinical and Experimental Dentistry*. 2019;11(2):e170.
4. Brauer M, Curtin JJ. Linear mixed-effects models and the analysis of non-independent data: A unified framework to analyze categorical and continuous independent variables that vary within-

- subjects and/or within-items. *Psychological Methods*. 2018;23(3):389-411.
5. Bas E, Yolcu U, Egrioglu E. Intuitionistic fuzzy time series functions approach for time series forecasting. *Granular Computing*. 2021;6(3):619-629.
 6. Khan SQ, Ahmed WMAW, Aleng NA. The development of regression modeling through design of experiment (doe) methodology: An overview the effect of bootstrapping data. *Sapporo Medical Journal*. 2121;55(10):2010215510396. Available:<https://www.maejournal.com/article/the-development-of-regression-modeling-through-design-of-experiment-doe-methodology-an-overview-the-effect-of-bootstrapping-data>
 7. Van-Kuijk SM, Dankers FJ, Traverso A, Wee L. Preparing data for predictive modelling. *Fundamentals of clinical data science*. 2019;75-84.
 8. Hesamian G, Akbari MG. A fuzzy additive regression model with exact predictors and fuzzy responses. *Applied Soft Computing*. 2020;95:106507.
 9. Klir G, Yuan B. Possibility theory. In *Handbook of Fuzzy Computation*. CRC Press. 2020; 185-B4.
 10. Feng X, Tan Q, Wei C. Hesitant fuzzy linguistic multi-criteria decision making based on possibility theory. *International Journal of Machine Learning and Cybernetics*. 2018;9(9):1505-17.
 11. Škrjanc I, Iglesias JA, Sanchis A, Leite D, Lughofer E, Gomide F. Evolving fuzzy and neuro-fuzzy approaches in clustering, regression, identification, and classification: a survey. *Information Sciences*. 2019;490:344-68.
 12. López S, Márquez AA, Márquez FA, Peregrín A. Evolutionary design of linguistic fuzzy regression systems with adaptive defuzzification in big data environments. *Cognitive Computation*. 2019;11(3):388-99.
 13. Ahmed WMAW, Khan SQ, Rohim RAA, Aleng NA, Ghazali FMM. Approximation of Randomized block design towards fuzzy multiple linear regression: A case study in health sciences. *International Journal of Scientific and Technology Research*. 2020;9(1):1303-8.
 14. Walpole RE, Myers RH, Myers SL, Ye K. *Probability & statistics for engineers & scientists* (7th Edition). Prentice Hall; 2006.
 15. Singh D, Singh B. Investigating the impact of data normalization on classification performance. *Applied Soft Computing*. 2020;97:105524.
 16. REF 1: Van-Kuijk SM, Dankers FJ, Traverso A, Wee L. Preparing data for predictive modelling. *Fundamentals of Clinical Data Science*. 2019;75-84.
 17. REF 2: Chen T, Shang C, Su P, Keravnou-Papailiou E, Zhao Y, Antoniou G, Shen Q. A decision tree-initialised neuro-fuzzy approach for clinical decision support. *Artificial Intelligence in Medicine*. 2021;111:101986.
 18. REF 3: Ahmad WM, Nawi MA, Aleng NA, Shafiq M. An Alternative Method for Multiple Linear Model Regression Modeling, a Technical Combining of Robust, Bootstrap and Fuzzy Approach. *Journal of Modern Applied Statistical Methods*. 2016;15(2):743-54.
 19. REF 4: GÜldoğan E, Zeynep TU, Ayça AC, Çolak C. Performance Evaluation of Different Artificial Neural Network Models in the Classification of Type 2 Diabetes Mellitus. *The Journal of Cognitive Systems*. 2020;5(1):23-32.
 20. REF 5: Ferenci T, Kovacs L. Predicting body fat percentage from anthropometric and laboratory measurements using artificial neural networks. *Applied Soft Computing*. 2018;67:834-9.
 21. REF 6: Ahmad WMAW, Rohim RAA, Ismail NH. Forecasting parameter estimates: A modeling approach using exponential and linear regression. *Engineering, Technology & Applied Science Research*. 2018;8(4):3162-3167.

© 2022 Khan and Ahmad; This is an Open Access article distributed under the terms of the Creative Commons Attribution License (<http://creativecommons.org/licenses/by/4.0>), which permits unrestricted use, distribution, and reproduction in any medium, provided the original work is properly cited.

Peer-review history:

The peer review history for this paper can be accessed here:

<https://www.sdiarticle5.com/review-history/82304>